

# General Physics (PHY 2130)

## Lecture 10

- Other types of friction forces, air resistance
- Connected objects. Tension.
- Reference frames.



# Lightning Review

## Last lecture:

1. Examples of application of Second Newton's Law
  - ✓ gravity and apparent weight
  - ✓ contact forces: normal force and friction

# Recall: Applying Newton's Laws

## ► Assumptions

- Objects behave as particles
  - can ignore rotational motion (for now)
- Masses of strings or ropes are negligible
- Interested only in the forces acting on the object

# Recall: Applying Newton's Laws

- ▶ Make a sketch of the situation described in the problem, **introduce a coordinate frame**
- ▶ Draw a **free body diagram** for the isolated object under consideration and label all the forces acting on it
- ▶ **Resolve the forces into x- and y-components**, using a convenient coordinate system
- ▶ **Apply equations**, keeping track of signs
- ▶ **Solve** the resulting equations



# Lightning Review

## Last lecture:

1. Examples of application of Second Newton's Law
  - ✓ gravity and apparent weight
  - ✓ contact forces: normal force and friction

**Review Problem:** A box full of books rests on a wooden floor. The normal force the floor exerts on the box is 250 N.

- (a) You push horizontally on the box with a force of 120 N, but it refuses to budge. What can you say about the coefficient of friction between the box and the floor?
- (b) If you must push horizontally on the box with 150 N force to start it sliding, what is the coefficient of static friction?

**Example:** A box full of books rests on a wooden floor. The normal force the floor exerts on the box is 250 N.

(a) You push horizontally on the box with a force of 120 N, but it refuses to budge. What can you say about the coefficient of friction between the box and the floor?

Apply Newton's 2<sup>nd</sup> Law

$$(1) \quad \sum F_y = N - w = 0$$

$$(2) \quad \sum F_x = F - f_s = 0$$

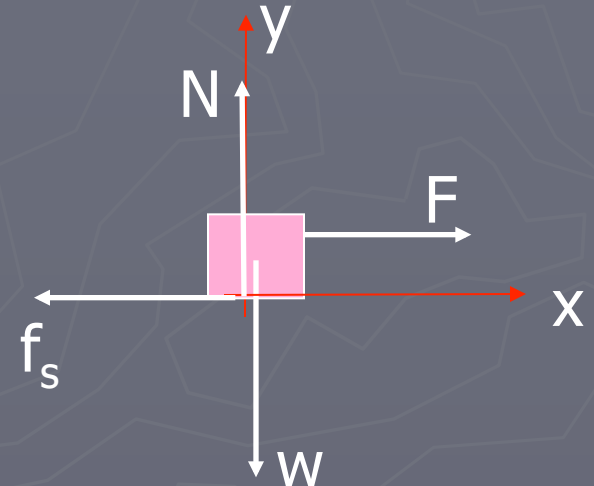
$$f_s \leq \mu_s N \quad \Rightarrow \quad \frac{f_s}{N} \leq \mu_s$$

The box refuses to budge,  $\Rightarrow \frac{f_s}{N} < \mu_s$

From (2):  $F = f_s \Rightarrow \frac{f_s}{N} = \frac{F}{N} = \frac{120\text{N}}{250\text{N}} = 0.48 < \mu_s$

$$\mu_s > 0.48.$$

FBD for box:



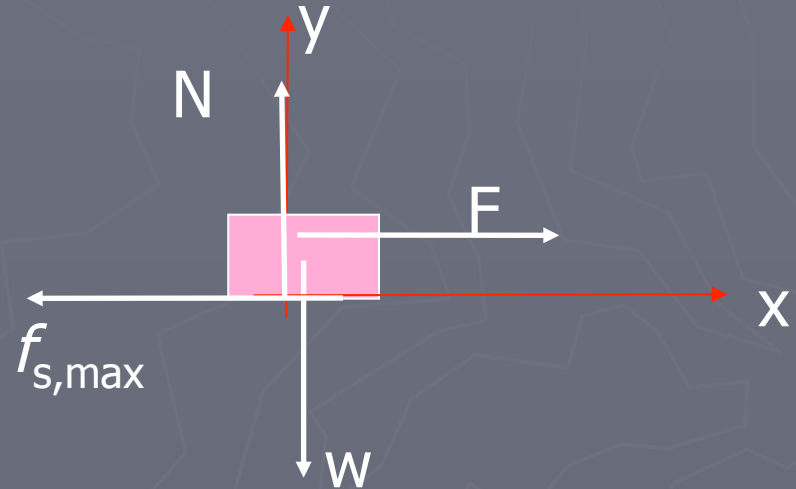
**(b) If you must push horizontally on the box with 150 N force to start it sliding, what is the coefficient of static friction?**

Apply Newton's 2<sup>nd</sup> Law

$$(1) \sum F_y = N - w = 0$$

$$(2) \sum F_x = F - f_{s,\max} = 0$$

$$f_s \leq \mu_s N \Rightarrow \frac{f_s}{N} \leq \mu_s$$



The box starts sliding, the friction force is  $f_{s,\max}$  here

From (2):  $F = f_{s,\max} \Rightarrow \mu_s = \frac{f_{s,\max}}{N} = \frac{F}{N} = \frac{150\text{N}}{250\text{N}} = 0.60$

$$\mu_s = 0.60.$$

### Example continued:

**(c) Once the box is sliding, you only have to push with a force of 120 N to keep it sliding. What is the coefficient of kinetic friction?**

FBD for box

Apply Newton's 2<sup>nd</sup> Law

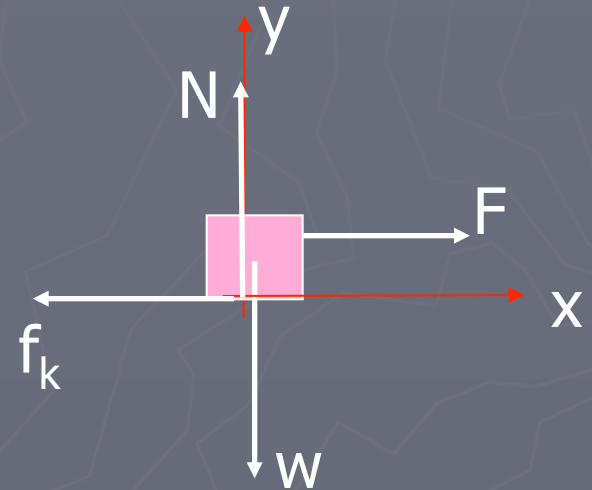
$$(1) \sum F_y = N - w = 0$$

$$(2) \sum F_x = F - f_k = 0$$

From 2:  $F = f_k = \mu_k N$

$$\mu_k = \frac{F}{N} = \frac{120 \text{ N}}{250 \text{ N}} = 0.48$$

$$\mu_k = 0.48$$

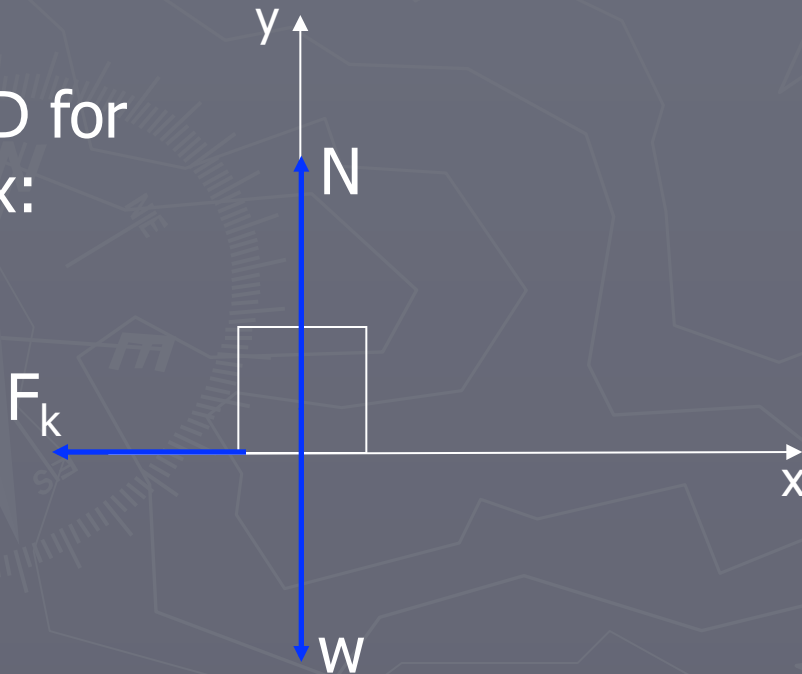




# Do you remember kinematics?

**Example:** A box slides across a rough surface. If the coefficient of kinetic friction is 0.3, what is the acceleration of the box? If the initial speed of the box is 10.0 m/s, how long does it take for the box to come to rest?

FBD for  
box:



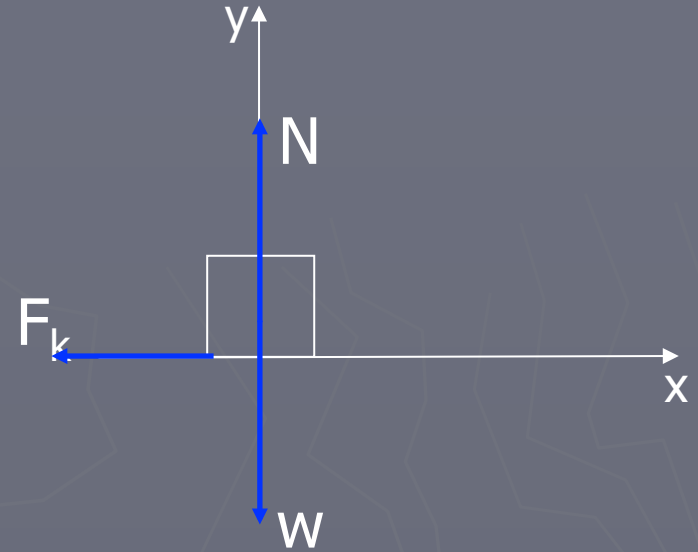
Apply Newton's 2<sup>nd</sup> Law:

$$\sum F_x = -F_k = ma$$

$$\sum F_y = N - W = 0$$

$$(1) -F_k = ma$$

$$(2) N - w = 0 \quad \therefore N = w = mg$$



$$\text{From (1): } -F_k = -\mu_k N = -\mu_k mg = ma$$

Solving for a:

$$a = -\mu_k g = -(0.3)(9.8 \text{ m/s}^2) = -2.94 \text{ m/s}^2$$

If the initial speed of the box is 10.0 m/s, how long does it take for the box to come to rest?

Given:

$$a = -2.94 \text{ m/s}^2,$$

$$v_{ix} = 10.0 \text{ m/s},$$

$$v_{fx} = 0.0 \text{ m/s}$$

Find:  $\Delta t = ?$

Solution:

$$v_{fx} = v_{ix} + a_x \Delta t = 0$$

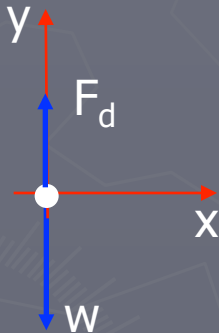
$$\Delta t = -\frac{v_{ix}}{a_x} = -\frac{+10.0 \text{ m/s}}{-2.94 \text{ m/s}^2} = 3.40 \text{ sec}$$

# Air Resistance and Terminal Speed

- ▶ Another type of friction is air resistance
- ▶ Air resistance is proportional to the speed of the object
- ▶ When the upward force of air resistance equals the downward force of gravity, the net force on the object is zero
- ▶ The constant speed of the object is the *terminal speed*

# Air Resistance

Imagine that a stone is dropped from the edge of a cliff. If air resistance *cannot* be ignored, the FBD for the stone is:



Apply Newton's Second Law

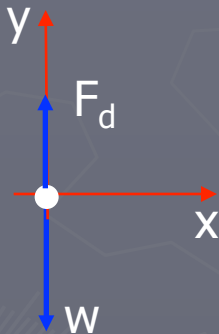
$$\sum F_y = F_d - w = ma$$

Where  $F_d$  is the magnitude of the drag force on the stone. This force is directed **opposite** the object's velocity.

Assume that  $F_d = bv^2$

$b$  is a parameter that depends on the size and shape of the object.

Since  $F_d \propto v^2$ , can the object be in equilibrium?



$$\sum F_y = F_d - w = ma$$

If  $a = 0$ , then

$$F_d - w = 0$$

$$bv^2 - mg = 0$$

Yes, the object can be in dynamic equilibrium, (moving with constant speed).

$$\text{when } v = v_t = \sqrt{\frac{mg}{b}}$$

$v_t$  is called terminal speed

**Example:** A paratrooper with a fully loaded pack has a mass of 120 kg. The force due to air resistance has a magnitude of  $F_d = bv^2$ , where  $b = 0.14 \text{ N s}^2/\text{m}^2$ .

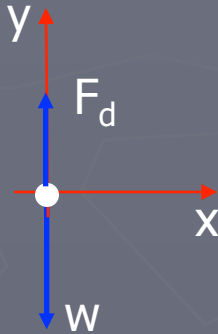
(a) If he/she falls with a speed of 64 m/s, what is the force of air resistance?

$$F_d = bv^2 = (0.14 \text{ N s}^2/\text{m}^2)(64 \text{ m/s})^2 = 570 \text{ N}$$

Example continued:

(b) What is the paratrooper's acceleration?

FBD:



Apply Newton's Second Law and solve for a.

$$\sum F_y = F_d - w = ma$$

$$a = \frac{F_d - mg}{m} = -5.1 \text{ m/s}^2$$

(c) What is the paratrooper's terminal speed?

$$\sum F_y = F_d - w = ma = 0$$

$$bv_t^2 - mg = 0$$

$$v_t = \sqrt{\frac{mg}{b}} = 92 \text{ m/s}$$



# Connected objects. Tension.

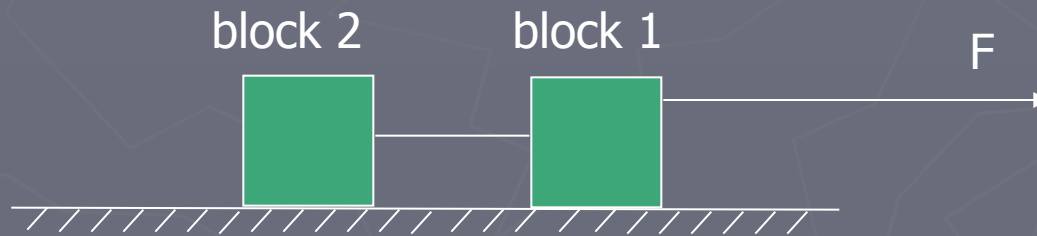


# Tension

**Tension** is the force transmitted through a “rope” from one end to the other.

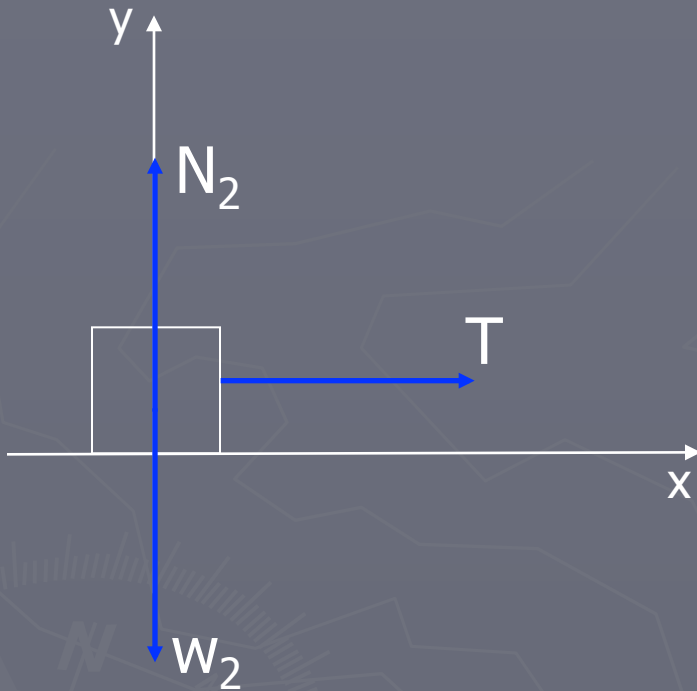
An **ideal** cord has zero mass, does not stretch, and the tension is the same throughout the cord.

**Example:** Find the tension in the cord connecting the two blocks as shown. A force of 10.0 N is applied to the right on block 1. Assume a frictionless surface. The masses are  $m_1 = 3.00$  kg and  $m_2 = 1.00$  kg.

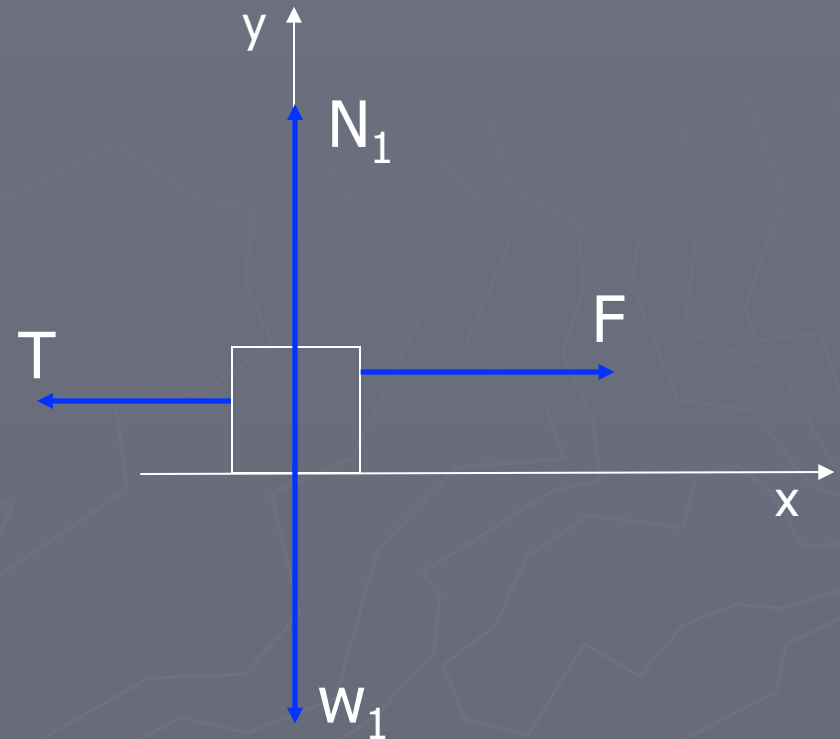


Assume that the rope stays taut so that both blocks have the same acceleration.

FBD for block 2:



FBD for block 1:



Apply Newton's 2<sup>nd</sup> Law to each block:

$$\sum F_x = T = m_2 a$$

$$\sum F_y = N_2 - w_2 = 0$$

$$\sum F_x = F - T = m_1 a$$

$$\sum F_y = N_1 - w_1 = 0$$

Example continued:

$$F - T = m_1 a \quad (1)$$

$$T = m_2 a \quad (2)$$

These two equations contain the unknowns:  $a$  and  $T$ .

To solve for  $T$ ,  $a$  must be eliminated. Solve for  $a$  in (2) and substitute in (1).

$$F - T = m_1 a = m_1 \left( \frac{T}{m_2} \right)$$

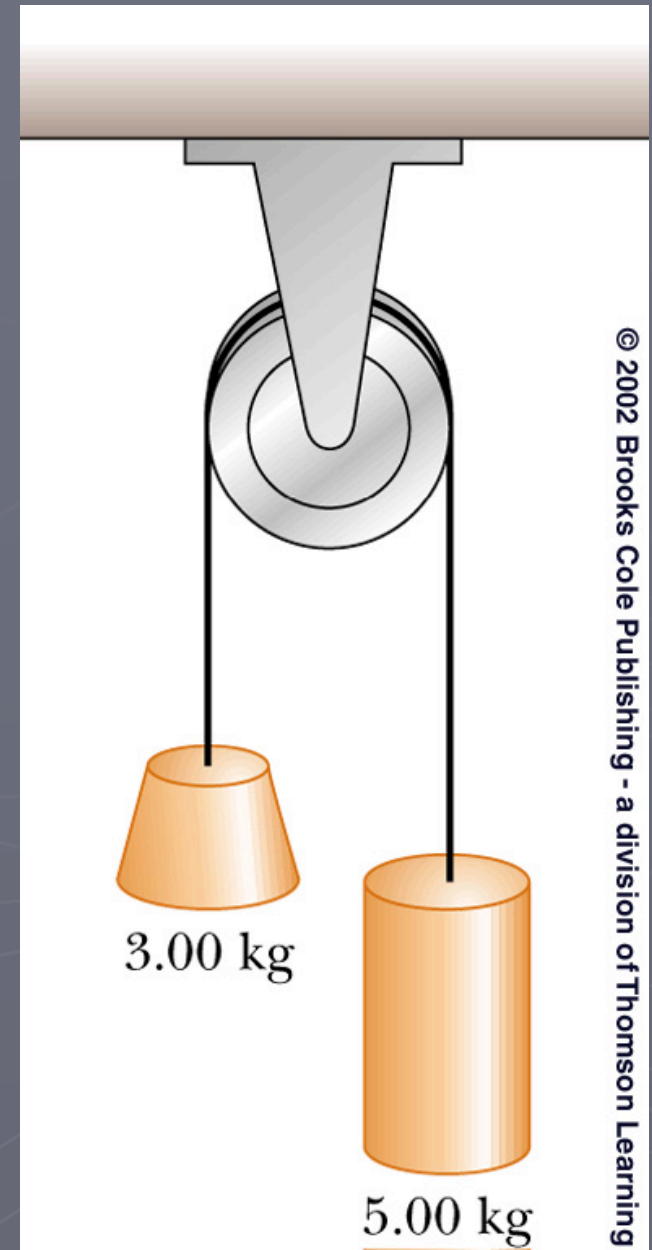
$$F = m_1 \left( \frac{T}{m_2} \right) + T = \left( 1 + \frac{m_1}{m_2} \right) T$$

$$\therefore T = \frac{F}{\left( 1 + \frac{m_1}{m_2} \right)} = \frac{10 \text{ N}}{\left( 1 + \frac{3 \text{ kg}}{1 \text{ kg}} \right)} = 2.5 \text{ N}$$

# Connected Objects

This example leads to the following observations/suggestions:

- ▶ Apply Newton's Laws separately to each object
- ▶ The acceleration of both objects will be the same
- ▶ The tension is the same in each diagram
- ▶ Solve the simultaneous equations



# More About Connected Objects

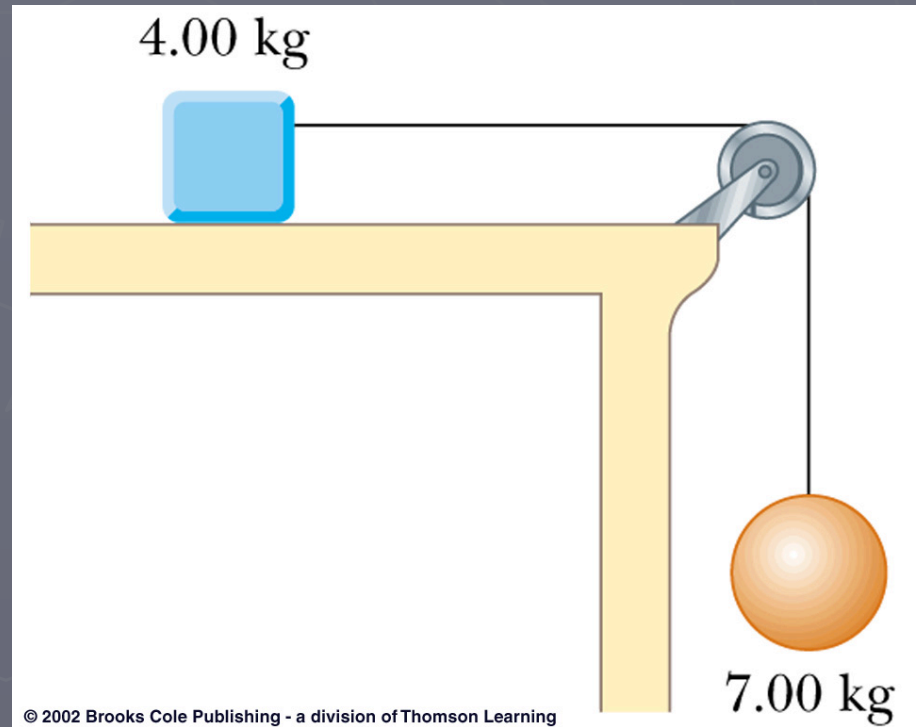
- ▶ Treating the system as one object allows an alternative method or a check
  - Use only external forces
    - ▶ Not the tension – it's internal
  - The mass is the mass of the system
- ▶ Doesn't tell you anything about any internal forces

# Example: Connected Objects

## Problem:

Two objects  $m_1 = 4.00 \text{ kg}$  and  $m_2 = 7.00 \text{ kg}$  are connected by a light string that passes over a frictionless pulley. The coefficient of sliding friction between the  $4.00 \text{ kg}$  object and the surface is  $0.300$ . Find the acceleration of the two objects and the tension of the string.

- ▶ Apply Newton's Laws **separately to each object**
- ▶ The **acceleration** of both objects will be **the same**
- ▶ The **tension is the same** in each diagram
- ▶ Solve the simultaneous equations





# Example: Connected Objects

Given:

mass1:  $m_1 = 4.00 \text{ kg}$

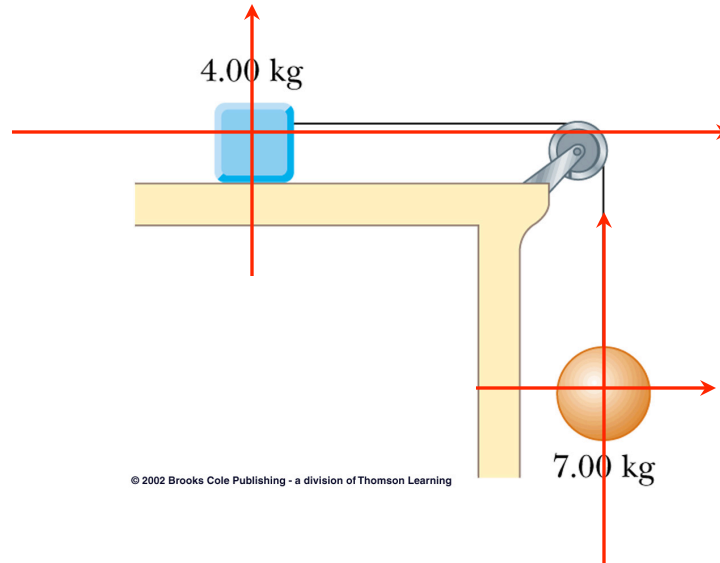
mass2:  $m_2 = 7.00 \text{ kg}$

friction:  $\mu = 0.300$

Find:

Tensions  $T = ?$

Acceleration  $a = ?$



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1. Introduce two coordinate frames:

Oy:  $y'$ 's are directed up

Ox:  $x'$ 's are directed right

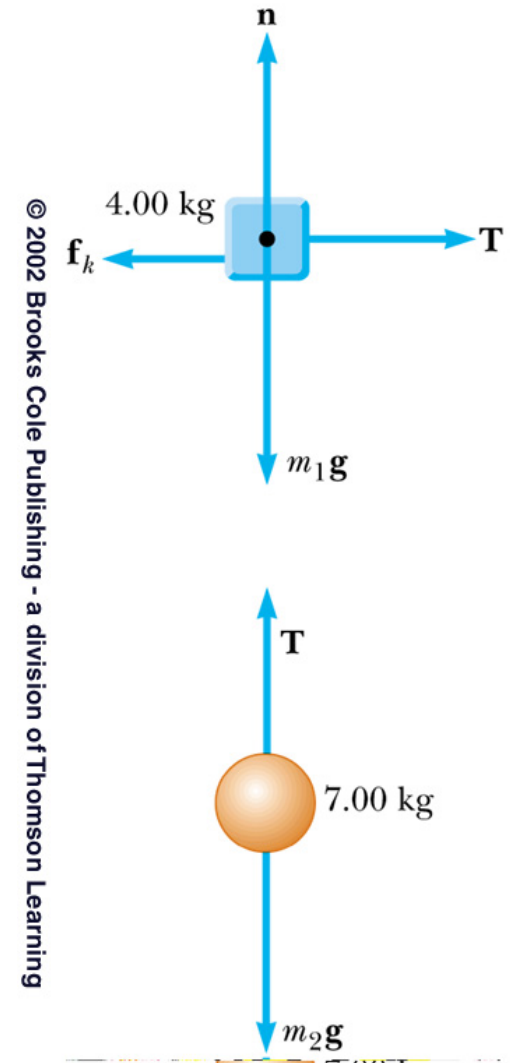
Note:  $\sum \vec{F} = m\vec{a}$ , and  $f_k = \mu n$

$$\left. \begin{array}{l} \text{Mass 1: } O_{x_1}: \sum F_x = T - f_k = m_1 a, \\ \quad \quad \quad O_{y_1}: \sum F_y = n - m_1 g = 0. \\ \text{Mass 2: } O_{y_2}: \sum F_y = m_2 g - T = m_2 a. \end{array} \right\}$$

Solving those equations:

$$a = 5.16 \text{ m/s}^2$$

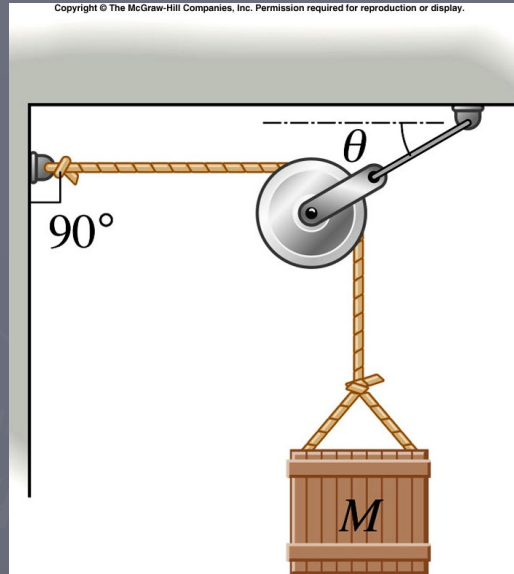
$$T = 32.4 \text{ N}$$



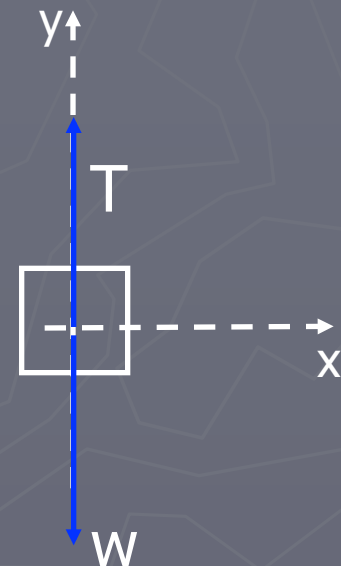
# More About Connected Objects

- ▶ Note that the forces could also be applied at an angle
  - It is very important to properly draw a FBD
  - It is very important to properly introduce a coordinate frame
  - It is very important to properly write components of the forces

**Example:** A pulley is hung from the ceiling by a rope. A block of mass 12 kg is suspended by another rope that passes over the pulley and is attached to the wall. The rope fastened to the wall makes a right angle with the wall. Neglect the masses of the rope and the pulley. Find the tension in the rope from which the pulley hangs and the angle  $\theta$ .



**FDB for the mass M**



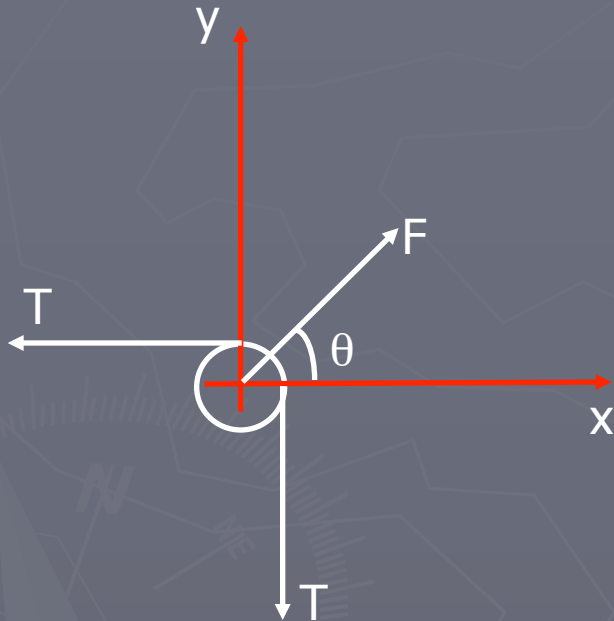
Apply Newton's 2<sup>nd</sup> Law to the mass M:

$$\sum F_y = T - w = 0$$

$$T = w = Mg = 12\text{kg} \times 9.8\text{m/s}^2 = 117.6\text{N}$$

Example continued:

FBD for the pulley:



Apply Newton's 2<sup>nd</sup> Law:

$$\sum F_x = F \cos \theta - T = 0$$

$$\sum F_y = F \sin \theta - T = 0$$

$$\therefore T = F \cos \theta = F \sin \theta$$

$$\tan \theta = 1 \Rightarrow \theta = 45^\circ$$

$$\begin{aligned} F &= \sqrt{2}T = \sqrt{2}Mg \\ &= \sqrt{2}(12\text{kg})(9.8\text{m/s}^2) \\ &= 166.3\text{ N} \end{aligned}$$

$$F = 166.3\text{ N and } \theta = 45^\circ$$

# Reference Frames

For Newton's Second Law to be valid it must be applied in an inertial reference frame. An inertial reference frame is one where Newton's First law is valid.